

We consider the complexification of the Boson-Fermion Fock space as representations of spaces of  $L^2$  complex differential forms. Within this framework, the Dolbeault type operators acting in those spaces, whose domains contain the space of polynomial type functionals, are introduced. Then, we derive integration by parts formulae for certain general complex differential forms on these operators. Applying these formulae, we have the complex version of the de Rahm-Hodge-Kodaira type decomposition on the Dolbeault type operators and a representation of the infinite dimensional Laplacian by these operators.